



# Preferential activation of CO near hydrocarbon chains during Fischer–Tropsch synthesis on Ru



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## ARTICLE INFO

### Article history:

Received 25 November 2015

Revised 14 January 2016

Accepted 16 January 2016

### Keywords:

Fischer–Tropsch synthesis

CO activation

C–C bond formation

Co-adsorbate interactions

Ruthenium

Coverage effects

## ABSTRACT

We report here theoretical evidence for an enhancement in CO activation to form  $C_1$  monomers at locations near growing hydrocarbon chains as a result of their ability to disrupt the dense monolayers of chemisorbed  $CO^*$  present during Fischer–Tropsch synthesis (FTS). These previously unrecognized routes become favored at the high  $CO^*$  coverages that prevail on curved cluster surfaces at conditions of FTS practice and account for the rapid growth of chains, which requires a source of vicinal monomers. CO activation initially requires a vacant site (and consequently  $CO^*$  desorption) and proceeds via  $CO^*$  reactions with  $H^*$  to form hydroxymethylene ( $CH^*OH^*$ ), which then dissociates to form  $OH^*$  and  $CH^*$ ;  $CH_x^*$  species can subsequently act as monomers and insert into chains, a process denoted as the ‘carbene’ mechanism. These  $CH^*$ , and their larger alkylidyne ( $C_nH_{2n-1}$ ) homologs, disrupt the dense  $CO^*$  adlayers and in doing so allow the facile formation of vicinal  $CH^*OH^*$  intermediates that mediate CO activation, without requiring, in this case,  $CO^*$  desorption. This causes  $CO^*$  activation effective enthalpy and free energy barriers to be  $\sim 100$  and  $\sim 15$   $\text{kJ mol}^{-1}$  lower, respectively, near growing chains than within unperturbed monolayers. These effects are observed near alkylidyne ( $C_nH_{2n-1}$ ) but not alkylidene ( $C_nH_{2n}$ ) or alkyl ( $C_nH_{2n+1}$ ) chains. These phenomena cause monomers to form preferentially near growing alkylidyne chains, instead of forming at undisrupted regions of  $CO^*$  monolayers, causing chain growth (via  $CH_x^*$ -insertion) to occur much more rapidly than chain initiation, a requirement to form long chains. Such routes resolve the seemingly contradictory proposals that  $CH_x^*$  species act as monomers (instead of  $CO^*$ ) and chain initiators, but their formation and diffusion on dense  $CO^*$  adlayers must occur much faster than chain initiation for such chains to grow fast and reach large average lengths. Chains disrupt surrounding molecules in the adlayer, causing faster monomer formation precisely at locations where they can readily react with growing chains. This work illustrates how interactions between transition states and co-adsorbates can dramatically affect predicted rates and selectivities at the high coverages relevant to practical catalysis.

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## 1. Introduction

Fischer–Tropsch synthesis (FTS) converts synthesis gas mixtures ( $CO$  and  $H_2$ ) to hydrocarbons on Fe, Co, and Ru catalysts [1–3]; it is a process critical to the success of many strategies for the conversion of natural gas, biomass, and  $CO_2$  to fuels, energy carriers, and chemicals. Hydrocarbon chains are initiated by CO

activation on metal surfaces; these chains propagate by adding CO-derived monomers and terminate via desorption as alkenes, alkanes, and mixtures of oxygenates [2–4]. Kinetic [5–7], infrared [8,9], isotopic switch [4], and theoretical studies [8] indicate that these reactions occur on surfaces nearly saturated with chemisorbed CO ( $CO^*$ ).

Recent studies have confirmed that CO activation occurs via H-assisted routes that form hydroxymethylene ( $CH^*OH^*$ ) species before the cleavage of the C–O bond on Co and Ru [6,8,10,11].  $CH^*OH^*$  dissociates to form  $CH^*$  species that hydrogenate to form  $CH_x^*$  (and ultimately  $CH_4$ ) or react with a  $CO^*$ -derived monomer ( $C_1^*$ ,  $CO^*$  or  $CH_x^*$ ) to form C–C bonds; the  $OH^*$  formed via  $CH^*OH^*$  dissociation results in  $H_2O$  co-products [6,8,10–12]. Such

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mechanistic consensus is not apparent for C–C bond formation routes.  $^{12}\text{CO}/^{13}\text{CO}$  isotopic switch data have shown that alkenes form with similar isotopic content at each location along the backbone, indicating that all of its C-atoms are added within a period of time much shorter than the time required to replace  $\text{CO}^*$  reactant with a given carbon isotope [4]. These data indicate that a small number of chains grow rapidly on surfaces during FTS, via a process that appears to require the rapid formation of monomers within diffusion distances from growing chains.

Hydrocarbon chains can react with vicinal  $\text{CO}^*$  in CO-insertion routes that form C–C bonds and  $\text{CH}_x\text{CO}^*$  species; the latter may desorb after H-addition to form alkanals and alkanols or cleave its C–O bond to form precursors to alkenes and alkanes [13–18]. The rapid chain growth processes discussed above could plausibly occur via  $\text{CO}^*$ -insertion because of readily available vicinal  $\text{CO}^*$  when chains grow on  $\text{CO}^*$ -saturated surfaces; theoretical treatments of such routes will be reported in a separate manuscript at a later time.

$\text{CH}_x^*$  addition to growing chains can also form C–C bonds, as inferred from the incorporation of  $\text{CH}_2^*$  species derived from  $\text{CH}_2\text{N}_2$  into the hydrocarbons formed from  $\text{H}_2$ –CO reactants [19,20], via a process that has been denoted as the carbene route [21–26]. These  $\text{CH}_x^*$  species form from  $\text{CO}^*$  via the same H\*-assisted CO cleavage that initiates chains. For fast chain growth [4], such  $\text{CH}_x$ -insertion propagation routes would require that CO activation steps be much faster than the corresponding steps that initiate chains and that  $\text{CH}_x^*$  species, some with multiple covalent surface attachments, diffuse very rapidly on  $\text{CO}^*$ -saturated surfaces.

Here, we provide theoretical evidence for an alternate route that involves the preferential H-assisted activation of  $\text{CO}^*$  molecules that reside next to a growing chain. Such processes are made possible through a disruption of dense  $\text{CO}^*$  monolayers by such growing chains, which lead to an “activation space”; this space avoids the need to desorb an additional  $\text{CO}^*$ , which carries a significant enthalpic penalty, to ameliorate the repulsive forces that destabilize transition states at high  $\text{CO}^*$  coverages. These first-principles density functional theory (DFT) calculations show that enthalpy and free energy barriers for H\*-assisted  $\text{CO}^*$  activation on Ru surfaces are lower for activating  $\text{CO}^*$  vicinal to hydrocarbon chains, via monolayer disruption phenomena that are likely to prevail at the  $\text{CO}^*$  coverages required for significant chain growth from  $\text{H}_2$ –CO reactants on other FTS catalysts. These seemingly unrecognized processes allow fast  $\text{CH}_x^*$  mediated chain propagation to readily occur via preferential monomer formation near growing chains and thus account for the rapid chain growth observed experimentally but inconsistent with the carbene route. More generally, the results presented herein indicate that dense adlayers, ubiquitous in the practice of catalysis, significantly influence the steric and electronic properties of sites and intermediates and thus the reactivity of adsorbates, an essential feature often ignored in fundamental studies carried out on model surfaces at low surface coverages.

## 2. Methods

Periodic plane-wave DFT methods implemented in the Vienna *ab initio* simulation package (VASP) [27–30] were used to calculate adsorption and reaction energies and activation barriers for elementary steps involved in  $\text{CO}^*$  activation and  $\text{CH}_x^*$  formation. Plane-waves were constructed using projector augmented-wave (PAW) potentials with an energy cutoff of 400 eV [31,32]. The revised Perdew–Burke–Ernzerhof (RPBE) form of the generalized gradient approximation (GGA) was used to determine exchange and correlation energies [33–35]. Furthermore, calculations were

carried out using optB86b-vdW [36] and vdW-DF2 [37] GGA functionals to describe dispersion forces among atoms. Similar dispersive interactions were incorporated into RPBE calculations using DFT-D3 with Becke and Johnson (BJ) damping [38,39]. DFT-D3 was also used to determine interactions among non-metal atoms (C, O, and H) to correct for dispersive interactions only between co-adsorbates, as the parameters for the DFT-D3 method were primarily based on interactions of gas-phase species [38,39]. Wavefunctions were converged to within  $10^{-6}$  eV and forces were computed using a fast Fourier transform (FFT) grid with a cutoff of twice the planewave cutoff. A  $1 \times 1 \times 1$  Monkhorst–Pack sampling of the first Brillouin zone (k-point mesh) was used [40] and structures were relaxed until forces on unconstrained atoms were  $<0.05$  eV/Å.

A 586-atom Ru cubo-octahedral particle ( $\sim 2.5$  nm in diameter) was used in the calculations at 1.044  $\text{CO}^*/\text{Ru}$  coverages (284  $\text{CO}^*$  on 272 surface Ru atoms) to account for sites with different coordinations and relevant  $\text{CO}^*$  coverages. Edge and corner atoms of low coordination (96 atoms) on  $\text{Ru}_{586}$  stabilized bridge-bound  $\text{CO}^*$  species (108  $\text{CO}^*$  species) that lead to supramonolayer coverages (Fig. 1) through the formation of geminal dicarbonyl species as observed with infrared experiments [8]. The high saturation coverages found here are fully consistent with in situ infrared studies [8,9,41], isotopic switch experiments [4], transient kinetic studies [6] and previous FTS kinetic studies [5–7] that all indicate that the Co and Ru surfaces are fully covered in  $\text{CO}^*$  at FTS conditions.  $\text{CO}^*$  peak intensities measured on Ru with in situ infrared spectroscopy no longer increase with increasing CO pressures above  $\sim 0.5$  kPa CO even at higher temperatures (548–598 K) than those associated with FTS ( $\sim 500$  K), indicating that surfaces are saturated at such pressures [41]. Furthermore CO hydrogenation rates on Ru obtained at near-methanation conditions (548–598 K and 0.01–10 kPa CO) show that hydrogenation becomes inhibited by CO (indicating  $\text{CO}^*$  coverages exceed 0.5 ML) at less than 0.1 kPa CO [41]. This is consistent with high-vacuum studies that indicate saturation coverages of  $\sim 0.9$  ML  $\text{CO}^*$  are reached at  $10^{-2}$  Torr [42]. Rigorous FTS kinetic studies on Ru [8] and Co [6] also show that the rates of FTS are inhibited by increasing CO pressure which is a direct result of the dominance of the  $K_{\text{CO}}(\text{CO})$  term in the denominator of the rate equation:

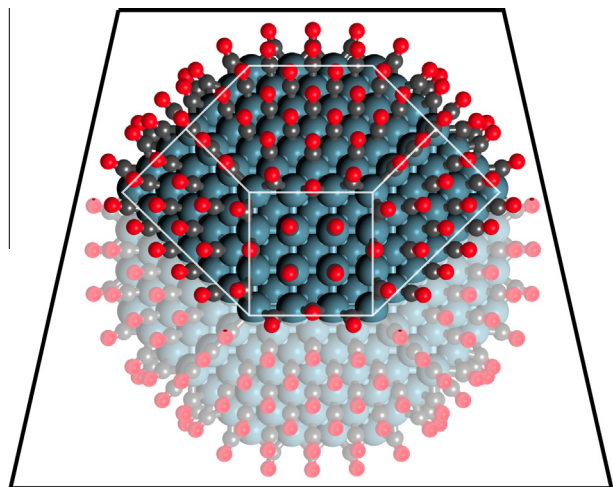
$$r = \frac{\alpha(\text{H}_2)(\text{CO})}{[1 + K_{\text{CO}}(\text{CO})]^2}$$

At conditions typical of FTS, the surface is fully covered in  $\text{CO}^*$  and thus  $K_{\text{CO}}(\text{CO})$  is  $\gg 1$ , leading to rates inversely proportional to CO pressure:

$$r = \frac{\alpha'(\text{H}_2)}{K_{\text{CO}}(\text{CO})}$$

The bottom six layers of the  $\text{Ru}_{586}$  cluster were removed along the (111) surface and the bottom two layers of this structure and their  $\text{CO}^*$  species were not allowed to relax during the calculations in order to decrease the computational demands and thus be able to explore a wider range of plausible intermediates and routes (Fig. 1). This  $\text{Ru}_{218}$  polycrystalline model was used for all calculations reported.

Transition state structures obtained for elementary steps were explored using nudged elastic band (NEB) methods [43,44] and then refined using dimer methods [45]. NEB methods used 16 images and wavefunctions converged to  $10^{-4}$  eV with a FFT grid 1.5 times the size of the plane-wave cutoff. Maximum forces on each atom were converged to  $<0.3$  eV/Å. The dimer algorithm was then used with wavefunctions converged to  $<10^{-6}$  eV and a FFT grid size twice the planewave cutoff and converged to a maximum force of  $<0.05$  eV/Å on each atom.



**Fig. 1.** Ru<sub>586</sub> nanoparticle at 1.044 ML CO\* along with the (111) plane used to cleave the catalyst model into a more computationally-feasible Ru<sub>218</sub> structure with four metal layers orthogonal to the closed-packed terrace.

Frequency calculations were carried out on all optimized states to determine zero-point vibrational energies (ZPVE), vibrational enthalpies ( $H_{\text{vib}}$ ), and free energies ( $G_{\text{vib}}$ ). Their values were used, together with VASP-derived electronic energies ( $E_0$ ), to obtain enthalpies:

$$H = E_0 + \text{ZPVE} + H_{\text{vib}} + H_{\text{trans}} + H_{\text{rot}} \quad (1)$$

and free energies:

$$G = E_0 + \text{ZPVE} + G_{\text{vib}} + G_{\text{trans}} + G_{\text{rot}} \quad (2)$$

for all reactant, product, and transition state structures. For RPBE GGA, the dispersion-corrected enthalpies:

$$H = E_0 + E_d + \text{ZPVE} + H_{\text{vib}} + H_{\text{trans}} + H_{\text{rot}} \quad (3)$$

and free energies:

$$G = E_0 + E_d + \text{ZPVE} + G_{\text{vib}} + G_{\text{trans}} + G_{\text{rot}} \quad (4)$$

were also calculated, where  $E_d$  is the dispersive energy between all C, O, and H atoms estimated by DFT-D3(BJ) methods [38,39]. For gaseous molecules, translational and rotational enthalpies and free energies were computed from statistical mechanics. The equations used to determine ZPVE,  $H_{\text{vib}}$ , and  $G_{\text{vib}}$  from vibrational frequencies for all species and  $H_{\text{trans}}$ ,  $H_{\text{rot}}$ ,  $G_{\text{trans}}$ , and  $G_{\text{rot}}$  from statistical mechanics formalisms for gas-phase molecules are reported in the Supporting Information (SI; Eqs. (S1)–(S13)).

### 3. Results and discussion

#### 3.1. Theoretical treatments of dense monolayers of chemisorbed CO on Ru particles

The construction and analysis of relevant surfaces and of the elementary steps that they mediate require that we consider the number, configurations and binding energies of the CO\* species that form the monomers involved in chain growth and that we do so on surfaces with CO\* coverages of practical interest. Particle models allow for a more rigorous examination of the effects of surface atom coordination and of surface and adsorbate relaxations without the unphysical lateral rigidity imposed by flat extended models [8,10]. FTS turnover rates on Co [2,46] and Ru [47] catalyst increase with increasing particle size and then reach constant values for particles larger than 10 nm, indicating that turnovers occur predominantly on low-index planes that prevail on larger particles.

Smaller particles contain significant fractions of defect sites that can activate CO\* to form strongly-bound C\* and O\* species which ultimately deactivate such particles and may lead to bulk oxidation [2]. DFT-calculated differential CO adsorption enthalpies and free energies ( $\Delta H_{\text{ads,CO}}$  and  $\Delta G_{\text{ads,CO}}$  (at 1 bar) without dispersion corrections) on low-index terraces of the Ru<sub>218</sub> particles at 1.044 CO\* ML coverages are  $-46 \text{ kJ mol}^{-1}$  and  $+36 \text{ kJ mol}^{-1}$  (at 500 K), respectively (Fig. 2). The positive  $\Delta G_{\text{ads,CO}}$  values would preclude CO\* adsorption at these coverages even at the high CO pressures of FTS ( $\sim 10 \text{ bar CO}$ ). These positive adsorption free energies reflect strong CO\*–CO\* repulsions, which are depicted visually in Fig. 2 by the overlapping van der Waals radii on such crowded surfaces.

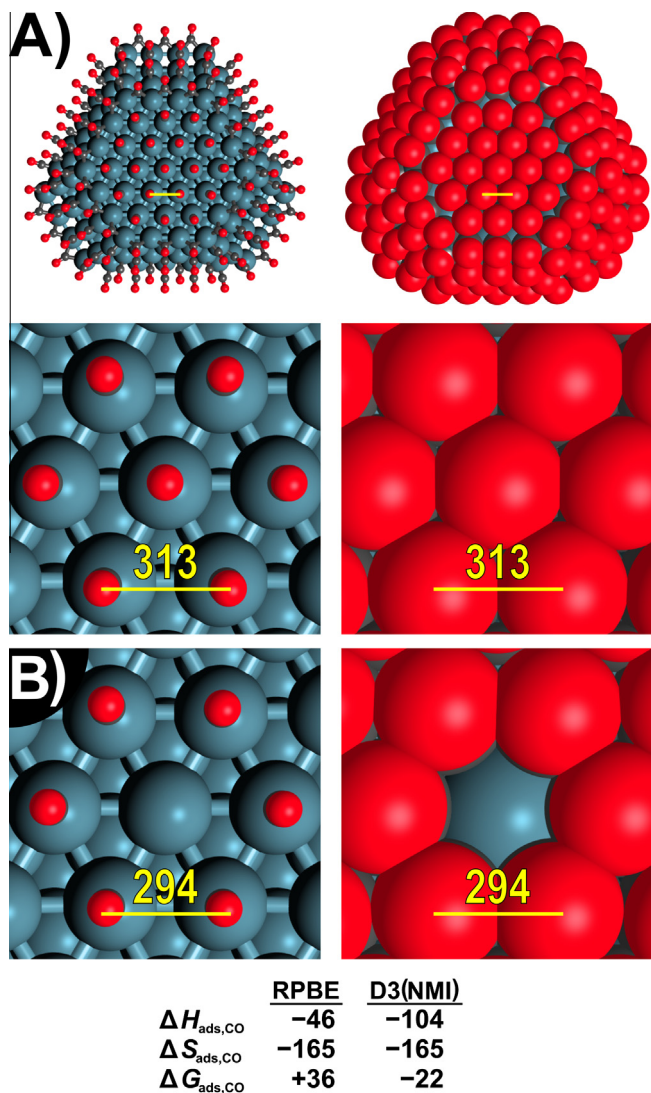
These DFT-derived energies, however, neglect dispersive CO\*–CO\* interactions and thus underestimate attractive induced dipole interactions between CO\* adsorbates, which, if included, stabilize CO\* species. These attractive forces are considered here by using empirical (DFT-D3) [38,39] and semi-empirical (optB86b-vdW [36] and vdW-DF2 [37] exchange correlation functionals) methods. These methods substantially lower the  $\Delta H_{\text{ads,CO}}$  and  $\Delta G_{\text{ads,CO}}$  values (by  $21\text{--}124 \text{ kJ mol}^{-1}$ ) relative to those from RPBE methods on surfaces with 1.044 ML CO\*, but do not detectably influence adsorption entropies ( $\Delta S_{\text{ads,CO}}$ ; Table 1). DFT-D3 methods give the strongest stabilization (decreasing both  $\Delta H_{\text{ads,CO}}$  and  $\Delta G_{\text{ads,CO}}$  by  $123 \text{ kJ mol}^{-1}$ ); while this empirical method can effectively model non-covalent interactions between gas-phase molecules [38,39], it has not been parametrized for the interactions between adsorbates and surface Ru atoms. Therefore, we include only dispersive interactions among co-adsorbates (non-metal atom interactions (NMI)); RPBE-D3(NMI) gives  $\Delta H_{\text{ads,CO}}$  and  $\Delta G_{\text{ads,CO}}$  values of  $-106 \text{ kJ mol}^{-1}$  and  $-23 \text{ kJ mol}^{-1}$  at 500 K, which are well within the range given by the other DFT methods such as PW-91/USPP and PBE/PAW methods used elsewhere [12–15,20], but are derived from methods which do not ‘overbind’ CO\* at low-coverages as PW-91 and PBE approaches do (Table 1) [35,48,49]. Also, the  $\Delta H_{\text{ads,CO}}$  and  $\Delta G_{\text{ads,CO}}$  values from RPBE-D3(NMI) are consistent with the high CO\* coverages detected by infrared spectroscopy [8,9,41], isotopic switch experiments [4], and kinetic data [5–7] at the conditions of FTS catalysis, as further discussed in Section 2. All enthalpies and free energies henceforth include  $E_d$  values estimated by D3(NMI) methods, using Eqs. (3) and (4) in Section 2, and all calculations are carried out within these dense monolayers on Ru<sub>218</sub> particles (1.044 ML CO\*).

#### 3.2. Chain initiation processes on CO\*-covered surfaces

We examine here how the presence of hydrocarbon chains disrupts these CO\* monolayers and, in doing so, influences H\*-assisted CO\* activation transition states. H-assisted CO\* activation requires quasi-equilibrated steps that form vacancies (via CO\* desorption, reverse of Step 1 in Scheme 1), CH\*O\* (via H-addition to CO\*, Step 3) and CH\*OH\* (via irreversible H-addition to CH\*O\*, Step 4), which dissociate to CH\* and OH\* (Step 5) that end up being removed as part of a chain and H<sub>2</sub>O products, respectively (Scheme 1). H<sub>2</sub> dissociation (Step 2) requires vacant metal atoms for its transition state, but at equilibrium, chemisorbed H-atoms (denoted as H') reside at three-fold sites within the dense CO\* adlayer and do not displace co-adsorbed CO\*. The presence of H' at a three-fold site vicinal to CO\* increases  $\Delta G_{\text{ads,CO}}$  values from  $-23 \text{ kJ mol}^{-1}$  to  $-13 \text{ kJ mol}^{-1}$  (500 K), an amount that is not sufficient to prevent CO\* adsorption at such sites at the CO pressures typical of FTS (10 bar CO).

The inability of H' to displace CO\* at low H' coverages is reflected in IR studies [6,8,9,41] that show CO\* peak intensities that are independent of H' coverage. This is also consistent with large free energies for dissociative H<sub>2</sub> chemisorption ( $\sim 40 \text{ kJ mol}^{-1}$ ) and low barriers for associative H' desorption ( $\sim 20 \text{ kJ mol}^{-1}$ )





**Fig. 2.** Calculated structures for (A) CO\*-covered Ru<sub>218</sub> particles and (B) vacancies at the center of the (111) terrace of Ru<sub>218</sub> particles with views (on right) illustrating the crowded nature of these surfaces by displaying atoms with their van der Waals radii. O–O bond distances between neighboring CO\* adsorbates are given in pm. Differential adsorption enthalpies ( $\Delta H_{\text{ads,CO}}$ , kJ mol<sup>-1</sup>), entropies ( $\Delta S_{\text{ads,CO}}$ , J mol<sup>-1</sup> K<sup>-1</sup>), and free energies ( $\Delta G_{\text{ads,CO}}$ , kJ mol<sup>-1</sup>) for CO\* are shown with (D3(NMI)) and without (RPBE) dispersion corrections.

which indicate quasi-equilibrated hydrogen adsorption. The low coverage of H' is also supported by a range of other kinetic studies that show FTS rates that are linearly proportional to H<sub>2</sub> pressure at all relevant H<sub>2</sub> pressures [2,5–8,10].

**Table 1**  
Differential adsorption enthalpies (kJ mol<sup>-1</sup>), Gibbs free energies (kJ mol<sup>-1</sup>), and entropies (J mol<sup>-1</sup> K<sup>-1</sup>) for CO\* on bare and CO\*-saturated (1.044 ML) low-index terraces of Ru<sub>218</sub> particles calculated using different functionals.

Functional	Potentials	0.004 ML CO* <sup>a</sup>			1.044 ML CO* <sup>a</sup>		
		$\Delta H$ (kJ mol <sup>-1</sup> )	$\Delta G$ (kJ mol <sup>-1</sup> )	$\Delta S$ (J mol <sup>-1</sup> K <sup>-1</sup> )	$\Delta H$ (kJ mol <sup>-1</sup> )	$\Delta G$ (kJ mol <sup>-1</sup> )	$\Delta S$ (J mol <sup>-1</sup> K <sup>-1</sup> )
RPBE	PAW	-151	-79	-144	-46	36	-165
RPBE-D3(NMI)	PAW	-151	-79	-144	-104	-22	-165
RPBE-D3	PAW	-193	-121	-144	-169	-87	-165
optB86b-vdW	PAW	-191	-120	-142	-138	-55	-165
vdW-DF2	PAW	-141	-70	-142	-67	13	-160
PBE	PAW	-175	-104	-142	-126	-45	-163
PW-91	USPP	-178	-100	-155	-96	-18	-156

<sup>a</sup> Coverages calculated based on 1 and 284 CO\* species on full Ru<sub>586</sub> nanoparticle cluster model.

H\*-assisted CO\* activation routes (Scheme 1) lead to a FTS rate equation consistent with reported rate data [2,5–8,10]:

$$r = \frac{\gamma K_{\text{CO}}(\text{CO})(\text{H}_2)}{[1 + K_{\text{CO}}(\text{CO})]^2} \quad (5)$$

where the  $K_{\text{CO}}$  represents the adsorption constants for CO (Step 1 in Scheme 1). In the context of the elementary steps depicted in Scheme 1, the value of  $\gamma$  is:

$$\gamma = K_{\text{H}_2} K_{\text{HCO}} k_{\text{HCOH}} \quad (6)$$

where  $K_{\text{H}_2}$  is the adsorption constant for H<sub>2</sub> (Step 2),  $K_{\text{HCO}}$  is the CH\*O\* formation equilibrium constant (Step 3) and  $k_{\text{HCOH}}$  is the rate constant for CH\*OH\* formation (Step 4). High CO\* coverages prevail at FTS conditions, resulting in  $K_{\text{CO}}(\text{CO}) \gg 1$  and:

$$r = \frac{\gamma(\text{H}_2)}{K_{\text{CO}}^2(\text{CO})} \quad (7)$$

where  $\gamma$  and  $K_{\text{CO}}$  can be written in terms of free energy differences as:

$$\frac{\gamma}{K_{\text{CO}}^2} = \frac{k_{\text{B}} T}{h} e^{\left(\frac{-\Delta G^\ddagger}{RT}\right)} \quad (8)$$

with

$$\Delta G^\ddagger = \Delta G^\ddagger_{\gamma} - \Delta G_{\text{ads,CO}} \quad (9)$$

$$\Delta G^\ddagger_{\gamma} = \Delta G_{\text{act,4}} + \Delta G_{\text{rxn,3}} + \Delta G_{\text{ads,H}_2} \quad (10)$$

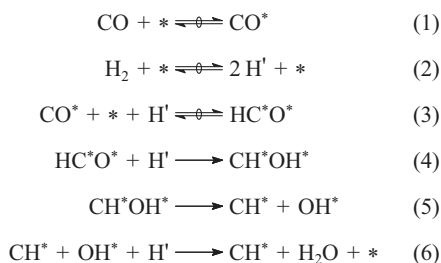
These equations can be rewritten in terms of the free energies of CH\*O\*–H' and CO\* and of gaseous species:

$$\Delta G^\ddagger_{\gamma} = G[\text{CH}^*\text{O}-\text{H}'] - G[\text{H}_2] - G[\text{CO}^*] - G[*] \quad (11)$$

$$\Delta G_{\text{ads,CO}} = G[\text{CO}^*] - G[*] - G[\text{CO}] \quad (12)$$

$\Delta G^\ddagger_{\gamma}$  thus represents the free energy of formation of the CH\*O–H' transition state from a surface with a single vacancy (along with the stoichiometric amounts of gaseous H<sub>2</sub>).

Fig. 3 depicts the DFT-derived reaction coordinate with reaction and activation enthalpies and free energies for H-assisted CO\*-activation routes. CO\* desorption forms a vacant site (reverse of Step 1) with  $-\Delta H_{\text{ads,CO}}$  and  $-\Delta G_{\text{ads,CO}}$  values of 104 and 22 kJ mol<sup>-1</sup>, respectively. Hydrogen is activated at this vacancy (Step 3) to form 2H' species, one of which reacts with CO\* to form CH\*O\* (which occupies two sites on the catalyst surface, Step 3) in an endothermic step ( $\Delta H_{\text{rxn}} = +79$  kJ mol<sup>-1</sup>,  $\Delta G_{\text{rxn}} = +82$  kJ mol<sup>-1</sup>). The barriers for CH\*O\* decomposition to H' and CO\* (reverse of Step 2, Scheme 1) are smaller (by 45 kJ mol<sup>-1</sup> in enthalpy and by 78 kJ mol<sup>-1</sup> in free energy) than for CH\*O\* reactions with H\* to form CH\*OH\* (Step 4), thus rendering Step 3 quasi-equilibrated. The formation of CH<sub>2</sub>O from CH\*O\* and H' has  $\Delta G^\ddagger$  of 226 kJ mol<sup>-1</sup>, slightly lower than that to form CH\*OH\*. The reverse free energy



**Scheme 1.** Mechanism for H-assisted CO\* activation via CH\*OH\* intermediates, where \* indicates a site which CO\* can occupy and ' indicates a three-fold site in which H' can bind without concomitant CO\* desorption.

barrier ( $158 \text{ kJ mol}^{-1}$ ) for  $\text{CH}_2\text{O}$  decomposition indicates that  $\text{CH}_2\text{O}$  is likely in equilibrium with CO and  $\text{H}_2$ . The equilibrium concentration of  $\text{CH}_2\text{O}$  will be very low at FTS conditions as the equilibrium constant is  $9 \times 10^{-5}$ , consistent with the presence of  $\text{CH}_2\text{O}$  as a trace product during FTS. The transition states for  $\text{CH}^*\text{OH}^*$  formation and for its dissociation (to  $\text{CH}^*$  and  $\text{OH}^*$ ) exhibit similar formation enthalpies ( $\Delta H^\ddagger = 234$  and  $233 \text{ kJ mol}^{-1}$ , respectively) and free energies ( $\Delta G^\ddagger$  of  $228 \text{ kJ mol}^{-1}$  and  $225 \text{ kJ mol}^{-1}$ , respectively). The similarities in these barriers make it impossible to determine the reversibility of  $\text{CH}^*\text{OH}^*$  formation. These two transition states are, however, kinetically-indistinguishable and lead to the same rate equation because of their similar stoichiometry; thus, the reversibility of  $\text{CH}^*\text{OH}^*$  formation does not affect the form of the observed rate equation (Eq. (8)), but only the mechanistic interpretation of  $\gamma$ .  $\text{CH}^*\text{OH}^*$  dissociation forms  $\text{CH}^*$  and  $\text{OH}^*$  and the latter reacts with  $\text{H}'$  to form  $\text{H}_2\text{O}$ , which desorbs from the surface creating a vacant site for CO to adsorb. The  $\Delta G^\ddagger$  for  $\text{CH}^*\text{O}-\text{H}^\ddagger$  formation is  $228 \text{ kJ mol}^{-1}$ , which comprises a  $\Delta G_\gamma^\ddagger$  of  $206 \text{ kJ mol}^{-1}$  and a  $\Delta G_{\text{ads, CO}}$  value  $-22 \text{ kJ mol}^{-1}$  (Fig. 3B). The overall reaction that converts  $\text{CO}^*$  and  $1.5 \text{ H}_2$  to  $\text{CH}^*$  and  $\text{H}_2\text{O}$  is exothermic ( $\Delta H_{\text{rxn}} = -23$  and  $\Delta G_{\text{rxn}} = -2 \text{ kJ mol}^{-1}$ , Fig. 4) and once a chain has been initiated (via  $\text{CH}^*$  formation), it can either terminate to form undesired  $\text{CH}_4$  or grow via  $\text{CO}^*$ - or  $\text{CH}_x^*$ -insertion mechanisms.

### 3.3. The formation of carbon–carbon bonds via $\text{CH}_x^*$ -insertion

The dearth of chains on working surfaces and their fast growth [4] may reflect direct  $\text{CO}^*$  insertion, which we consider in a later study. Alternatively,  $\text{CH}_x^*$  monomers or growing  $\text{RCH}_x^*$  chains may decrease the free energy of the transition state for  $\text{H}'$  addition

to  $\text{CH}^*\text{O}^*$  (referenced to its relevant precursor), specifically by avoiding the need to remove an additional  $\text{CO}^*$  to form this transition state.

The ratio of the rate of chain growth (C–C bond formation) to chain initiation ( $\text{CO}^*$  activation) is simply given by:

$$\frac{r_{\text{growth}}}{r_{\text{init}}} = \bar{n} - 1 \quad (13)$$

where ( $\bar{n}$ ) represents the average number of C-atoms in the products formed; this value is typically  $>10$  for practical Fischer–Tropsch synthesis. The rate of chain initiation is given by Eq. (5) in which  $\gamma$  is the lumped rate constant for



which ultimately leads to  $\text{CH}^*$  species on the catalyst surface (Step 5 in Scheme 1). Once two  $\text{CH}^*$  species are co-adsorbed, they can react to form a new C–C bond:

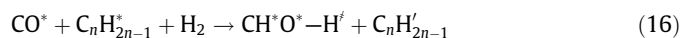


The intrinsic activation enthalpies and free energies ( $\Delta H_{\text{act}}$  and  $\Delta G_{\text{act}}$  of  $88$  and  $94 \text{ kJ mol}^{-1}$ , respectively, Fig. 5) are much smaller than the effective activation enthalpies and free energies for  $\text{CO}^*$  activation ( $230$  and  $235 \text{ kJ mol}^{-1}$ ), indicating that  $\text{CH}_x^*$ -insertion reactions are limited by the high activation free energies for forming vicinal  $\text{CH}_x^*$  species, rather than the activation free energies for C–C bond formation.

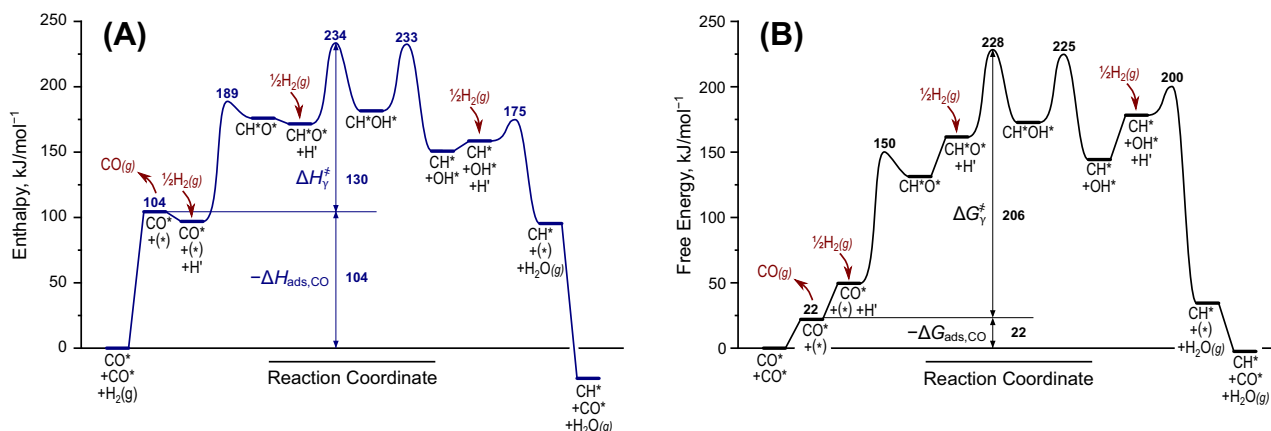
Alternative  $\text{CH}_x^*$ -insertion steps, such as the reactions of  $\text{CH}^*$  with  $\text{CH}_2^*$  or  $\text{CH}_3^*$ , and the  $\text{H}'$ -addition steps that ultimately form olefin and paraffin products are currently being examined using the same theoretical approaches utilized herein as part of a separate study.

### 3.4. $\text{CO}^*$ activation on dense $\text{CO}^*$ monolayers disrupted by growing chains

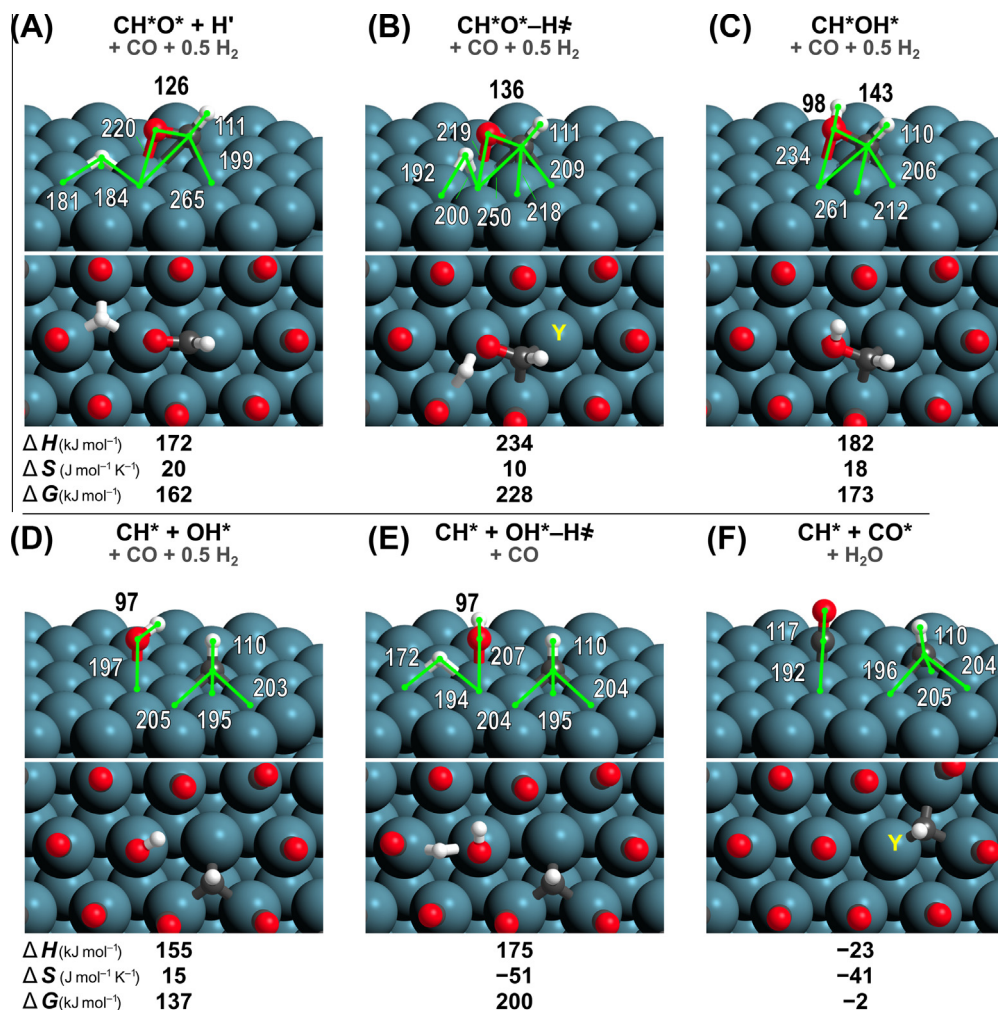
The rate of chain-growth is not limited by C–C bond formation, as these steps occur readily among vicinal hydrocarbon chains and  $\text{CH}_x^*$  monomers, as shown in Section 3.3. Instead, growth rates are limited by  $\text{CO}^*$  activation (to form  $\text{CH}_x^*$  monomers) at sites vicinal to growing chains (of length  $n$ )



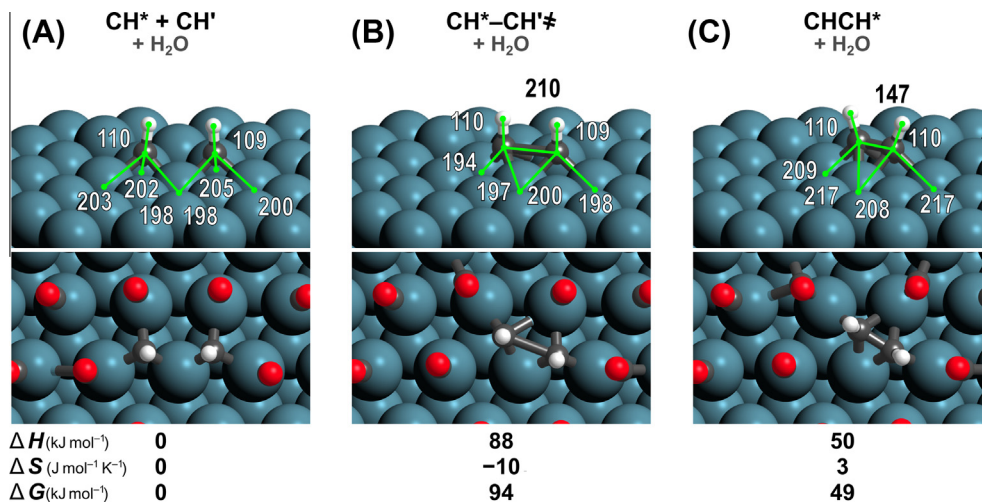
where the vicinal chain (shown as  $\text{CH}^*$  in Fig. 4F) and  $\text{CH}^*\text{O}^* - \text{H}^\ddagger$  transition states (Fig. 4B) share a metal atom site on the catalyst



**Fig. 3.** (A) Enthalpy and (B) free energy diagrams for  $\text{H}'$ -assisted CO activation (chain initiation) on  $\text{Ru}_{218}$  nanoparticles at  $1.04 \text{ ML CO}^*$ . Effective enthalpy and free energy barriers ( $\Delta H^\ddagger$  and  $\Delta G^\ddagger$  (Eq. (9))) reflect the  $\Delta H$  and  $\Delta G$  to form transition states from  $\text{CO}^*$ -covered surfaces and stoichiometric amounts of  $\text{H}_2(\text{g})$  and are shown for each transition state.  $\Delta H^\ddagger$  and  $\Delta G^\ddagger$  (Eq. (10)) represent the enthalpy and free energies to form the  $\text{CH}^*\text{O}-\text{H}^\ddagger$  from  $\text{CO}^*$  and a vicinal vacancy (\*). Electronic energy differences and zero-point corrections are shown in the SI (Table S1).



**Fig. 4.** DFT-derived structures for (A)  $\text{CH}^*\text{O}^* + \text{H}^*$ , (B)  $\text{CH}^*\text{O}^*-\text{H}^\ddagger$ , (C)  $\text{CH}^*\text{OH}^*$ , (D)  $\text{CH}^* + \text{OH}^*$ , (E)  $\text{CH}^* + \text{OH}^*-\text{H}^\ddagger$ , and (F)  $\text{CH}^* + \text{CO}^*$  along with enthalpies, entropies and free energies to form those states (along with stoichiometric amounts of gas-phase species) from a  $\text{CO}^*$ -covered surface. Top pictures omit spectating  $\text{CO}^*$  species for clarity and have bond distances labeled in pm. Structures for all states in Fig. 3 shown in the SI (Figs. S1–S5).



**Fig. 5.** DFT-derived structures for the (A)  $\text{CH}^* + \text{CH}^*$ , (B)  $\text{CH}^*-\text{CH}^\ddagger$ , and (C)  $\text{CHCH}^*$  along with enthalpies, entropies and free energies to form the transition and product states from the reactant precursor. Top pictures omit spectating  $\text{CO}^*$  species for clarity and have bond distances labeled in pm.



surface (labeled 'Y' in Fig. 4). The same sequence of elementary steps (Steps 2–6 in Scheme 1) leads to  $\text{CH}^*\text{O}^*-\text{H}^\ddagger$  formation in Eqs. (14) and (16). The rate of chain growth (limited by Eq. (15)) can thus be written as:

$$r_{\text{growth}} = \frac{\gamma_n K_{\text{CO}}(\text{CO})(\text{H}_2)[\text{C}_n^*]}{1 + K_{\text{CO}}(\text{CO})} \quad (17)$$

where  $[\text{C}_n^*]$  is the concentration of chains with length  $n$ . For each individual chain, Eqs. (5) and (17) can be rewritten as:

$$\frac{r_{\text{growth}}}{r_{\text{init}}[\text{C}_n^*]} = \frac{\gamma_n K_{\text{CO}}(\text{CO})}{\gamma_0} \quad (18)$$

at high CO pressures ( $K_{\text{CO}}(\text{CO}) \gg 1$ ), where  $\gamma_0$  and  $\gamma_n$  are the lumped rate constants for the steps in Eqs. (14) and (16). These  $\gamma$  parameters can be written in terms of free energy differences:

$$\gamma_i = \frac{k_B T}{h} \exp\left(\frac{-\Delta G_{yi}}{RT}\right) \quad (19)$$

which can be rewritten in terms of the free energies of the  $\text{CH}^*\text{O}^*-\text{H}^\ddagger$ ,  $\text{CO}^*$ , and gas-phase species:

$$\Delta G_{y0}^\ddagger = G[\text{CH}^*\text{O}^*-\text{H}^\ddagger] - G[\text{H}_2] - G[\text{CO}^*] - G[\text{C}_n^*] \quad (20)$$

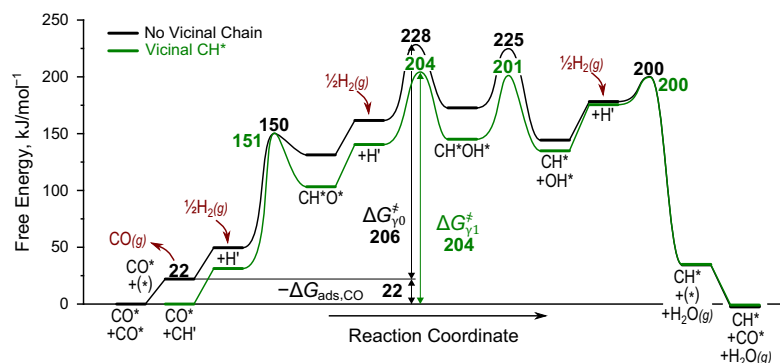
$$\Delta G_{yn}^\ddagger = G[\text{CH}^*\text{O}^*-\text{H}^\ddagger] - G[\text{H}_2] - G[\text{CO}^*] - G[\text{C}_n^*] \quad (21)$$

These free energies are calculated from DFT with ( $\Delta G_{yn}^\ddagger$ ) and without ( $\Delta G_{y0}^\ddagger$ ) a vicinal hydrocarbon chain.

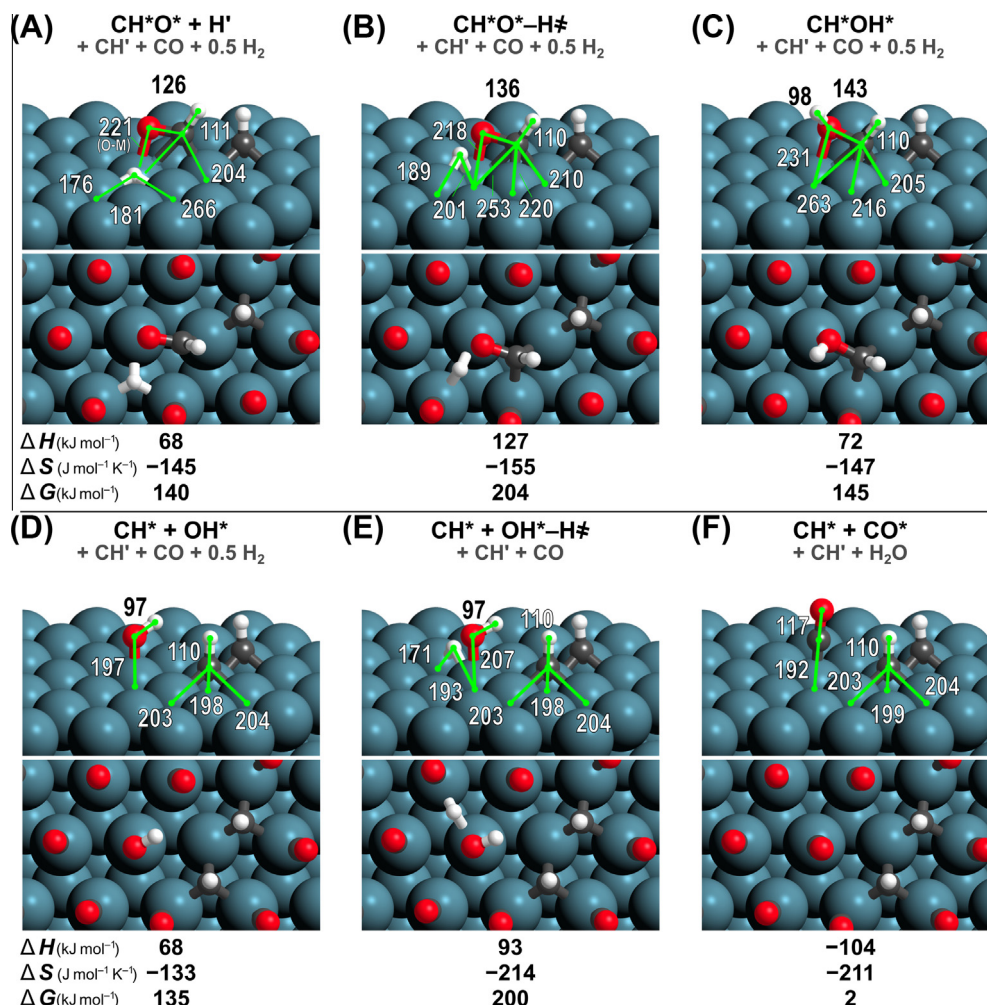
First, we examine the activation of a  $\text{CO}^*$  vicinal to a bound  $\text{CH}^*$ . Fig. 4F shows that  $\text{CH}^*$  binds to a three-fold site, preserving space in the  $\text{CO}^*$ -monolayer on the catalyst surface directly above metal atom 'Y'.  $\text{CO}^*$  adsorption at this site (Y) has a large positive  $\Delta G_{\text{ads,CO}}$  (+21 kJ mol<sup>-1</sup>), indicating that  $\text{CO}^*$  adsorption is unlikely to occur, even at the typical CO pressures (10 bar) in FTS. This space in the  $\text{CO}^*$ -monolayer above metal atom (Y), however, can accommodate the  $\text{CH}^*\text{O}^*-\text{H}^\ddagger$  transition state, as discussed in the next section. Fig. 5 shows DFT-derived reaction and activation free energies for H-assisted  $\text{CO}^*$  activation vicinal to  $\text{CH}^*$  and for the H-assisted path within dense  $\text{CO}^*$  monolayers without the disruptions by  $\text{CH}^*$  species. The steps that initiate such chains within  $\text{CO}^*$  monolayers require  $\text{CO}^*$  desorption to create the space necessary to form and bind  $\text{CH}^*\text{O}^*-\text{H}^\ddagger$  transition state structures, as discussed in Section 3.2. In contrast,  $\text{CO}^*$  activation vicinal to a chain does not require  $\text{CO}^*$  desorption, as the chain effectively prevents  $\text{CO}^*$  adsorption at such nearby sites and preserves the vacancy. Except for the lack of this CO desorption requirement ( $\Delta G_{\text{des,CO}}$

(+22 kJ mol<sup>-1</sup>)), the chain-assisted  $\text{CO}^*$  activation proceeds via the same elementary steps as those for chain initiation on dense  $\text{CO}^*$  monolayer surfaces (Steps 2–6 in Scheme 1). The free energy of activation to form  $\text{CH}^*\text{O}^*-\text{H}^\ddagger$  from  $\text{CO}^*$  and  $\text{H}_2$  with a co-adsorbed  $\text{CH}^*$  species ( $\Delta G_{y1}^\ddagger$ ) is 204 kJ mol<sup>-1</sup>, whereas the same reaction vicinal to a vacancy results in a similar value ( $\Delta G_{y0}^\ddagger$  of 206 kJ mol<sup>-1</sup>), leading to a decrease in the overall free energy barrier ( $\Delta G^\ddagger$ ) of 24 kJ mol<sup>-1</sup> for  $\text{CH}^*$ -assisted  $\text{CO}^*$  activation (Fig. 6). The small changes in  $\Delta G_{yi}^\ddagger$  with co-adsorbed  $\text{CH}^*$  ( $\Delta G_{y1}^\ddagger$ ) and without a co-adsorbed  $\text{CH}^*$  ( $\Delta G_{y0}^\ddagger$ ) indicate that lateral interactions between  $\text{CH}^*\text{O}^*-\text{H}^\ddagger$  and  $\text{CH}^*$  are weak (<3 kJ mol<sup>-1</sup>) as further demonstrated by similar  $\text{CH}^*\text{O}^*-\text{H}^\ddagger$  geometries (Figs. 4B and 7B). The weak lateral interactions between  $\text{CH}^*$  and the  $\text{CH}^*\text{O}^*-\text{H}^\ddagger$  are unique to that reaction, as co-adsorbate interactions between  $\text{CH}^*$  and the transition states for forming both  $\text{CH}^*\text{O}^*$  and  $\text{H}_2\text{O}^*$  are significant, leading to similar  $\Delta G^\ddagger$  values for those reactions during  $\text{CH}^*$ -assisted and non-assisted paths. The rate of  $\text{CO}^*$  activation, however, is ultimately dependent on the stabilities of the  $\text{CH}^*\text{O}^*-\text{H}^\ddagger$  transition state, making these other transition states (or their interactions with vicinal chains) irrelevant to rates of  $\text{CO}^*$  activation. The differences in the overall apparent activation energy for the non-assisted ( $\Delta G_0^\ddagger$ ) (-24 kJ/mol) and the  $\text{CH}^*$ -assisted ( $\Delta G_1^\ddagger$ ) path (+24 kJ mol<sup>-1</sup>) are predominantly due to the free energy required to desorb  $\text{CO}^*$  ( $\Delta G_{\text{des,CO}}$ , +22 kJ mol<sup>-1</sup>) to create the vacancy necessary to activate  $\text{CO}^*$  on the non-assisted surface.

Furthermore, the difference between  $\Delta G_0^\ddagger$  and  $\Delta G_1^\ddagger$  was also computed for the optB86b-vdW functional (with PAW potentials) and the PW-91 functional (with USPP pseudopotentials) in order to benchmark the novel RPBE-D3(NMI) method presented here against more widely-used methods. The PW-91 functional predicted a difference between  $\Delta G_0^\ddagger$  and  $\Delta G_1^\ddagger$  of 30 kJ mol<sup>-1</sup> while the optB86b-vdW method predicted a difference of 38 kJ mol<sup>-1</sup> (Table S1, SI). The positive differences in free energy barriers by these methods are consistent with the difference (+24 kJ mol<sup>-1</sup>) predicted by RPBE-D3(NMI), indicating that the conclusions herein are not dependent upon the choice of a unique functional. Furthermore, the differences between  $\Delta G_0^\ddagger$  and  $\Delta G_1^\ddagger$  for all three methods (24 kJ mol<sup>-1</sup>, 30 kJ mol<sup>-1</sup>, 38 kJ mol<sup>-1</sup> for D3(NMI), PW-91, and optB86b-vdW) are similar to the  $\Delta G_{\text{des,CO}}$  predicted by those methods (22 kJ mol<sup>-1</sup>, 18 kJ mol<sup>-1</sup>, and 55 kJ mol<sup>-1</sup> for D3(NMI), PW-91, and optB86b-vdW) as shown in Fig. S10 (SI). This relationship between ( $\Delta G_0^\ddagger$  and  $\Delta G_1^\ddagger$ ) and  $\Delta G_{\text{des,CO}}$  indicates that DFT methods which predict positive free energies for desorbing  $\text{CO}^*$  (such as the widely-used PBE method, Table 1) will also predict positive



**Fig. 6.** Comparison of the free energy diagrams for the  $\text{H}^*$ -assisted  $\text{CO}^*$  activation without a vicinal chain (black curve) and the  $\text{CH}^*$  promoted  $\text{H}^*$ -assisted  $\text{CO}^*$  activation (green curve) on Ru nanoparticles at 1.044 ML  $\text{CO}^*$ . Effective free energy barriers ( $\Delta G^\ddagger$ ) are the  $\Delta G$  to form transition states from their respective 'reference' states and stoichiometric amounts of  $\text{H}_2$  and are shown for each transition state. Labels for each state are simplified for clarity, but full labels can be seen in Fig. 3. Enthalpy differences (along with electronic energies and zero-point corrections) are shown in the SI (Tables S1 and S2).



**Fig. 7.** DFT-calculated structures for (A)  $\text{CH}^*\text{O}^* + \text{H}^* + \text{CH}^*$ , (B)  $\text{CH}^*\text{O}^*-\text{H}^* + \text{CH}^*$ , (C)  $\text{CH}^*\text{OH}^* + \text{CH}^*$ , (D)  $\text{CH}^* + \text{OH}^* + \text{CH}^*$ , (E)  $\text{CH}^* + \text{OH}^*-\text{H}^* + \text{CH}^*$ , and (F)  $\text{CH}^* + \text{CO}^* + \text{CH}^*$  along with enthalpies, entropies and free energies to form those states (along with stoichiometric amounts of gas-phase species) from  $\text{CO}^* + \text{CH}^*$  (Fig. 4F). Top pictures omit spectating  $\text{CO}^*$  species for clarity and have bond distances labeled in pm. Structures for all states in Fig. 6 shown in the SI (Figs. S6–S9).

differences between  $\Delta G_0^i$  and  $\Delta G_1^i$ , leading to conclusions consistent with those presented herein for the novel D3(NMI) approach.

To assess the effects of hydrocarbon chain length on the free energy barrier to form the  $\text{CH}^*\text{O}^*-\text{H}^*$  transition state vicinal to a growing chain ( $\Delta G_{\gamma i}^\ddagger$ ,  $i > 0$ ),  $\text{CO}^*$  activation was also examined vicinal to  $\text{CH}_3\text{C}^*$ ,  $\text{C}_2\text{H}_5\text{C}^*$ , and  $\text{C}_3\text{H}_7\text{C}^*$  ( $\text{CO}^*$  activation vicinal to alkylidene and alkylidyne chains is discussed in Section 3.4). The average  $\Delta G_\gamma^\ddagger$  for  $\text{CH}^*\text{O}^*-\text{H}^*$  formation vicinal to an alkylidyne chain ( $\text{C}_1-\text{C}_4$ ) is 213 kJ mol<sup>-1</sup>, as shown in Fig. 8B, slightly higher than for  $\text{CH}^*$  species ( $\Delta G_{\gamma 1}^\ddagger = 206$  kJ mol<sup>-1</sup>), leading to the ratio of lumped rate constants for  $\text{CO}^*$  activation ( $\gamma_n/\gamma_0$  in Eq. (18)) of  $\sim 0.2$  at 500 K, which then simplifies to:

$$\frac{r_{\text{growth}}}{r_{\text{init}}[\text{C}_n]} = 0.2 K_{\text{CO}}(\text{CO}) = 0.2 \exp\left(\frac{-\Delta G_{\text{ads,CO}}}{RT}\right)(\text{CO}) \quad (22)$$

at high  $\text{CO}^*$  coverages ( $K_{\text{CO}}(\text{CO}) \gg 1$ ) inferred from experiments or estimated from DFT ( $\Delta G_{\text{ads,CO}} = -22$  kJ mol<sup>-1</sup>, Eq. (12)), resulting in large ratios of chain growth to chain initiation via  $\text{CO}^*$  activation enhanced by vicinal hydrocarbon chains.

The ability of growing chains to promote the local activation of  $\text{CO}^*$  leads to a rate equation modified from Eq. (5) to add  $\text{CO}^*$  consumption vicinal to growing chains:

$$r_{\text{CO}} = \frac{\gamma_0 K_{\text{CO}}(\text{CO})(\text{H}_2)}{[1 + K_{\text{CO}}(\text{CO})]^2} \left( 1 + \alpha_1 \sum_{n=1}^{\infty} \left( \frac{\gamma_n}{\gamma_1} \right) \prod_{i=1}^n \alpha_{i-1} \right) \quad (23)$$

derived in the SI (by employing a pseudo-steady-state hypothesis on  $\text{C}_i^*$ , Eqs. (S14)–(S26)), where  $\alpha$  is the chain growth probability:

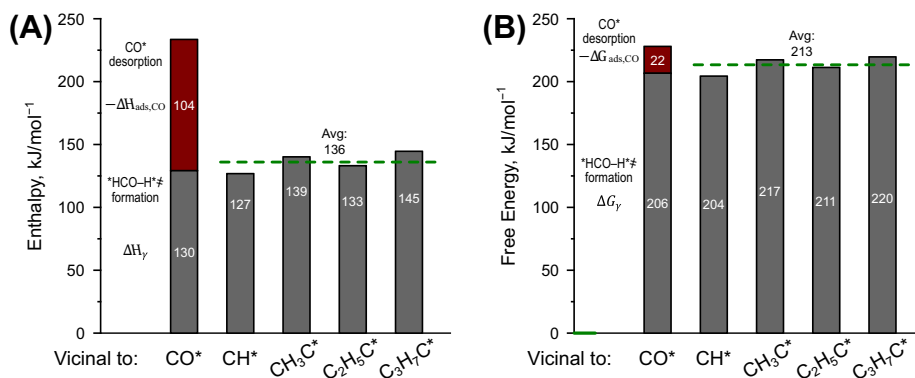
$$\alpha_i = \frac{r_{\text{growth},i}}{r_{\text{growth},i} + r_{\text{term},i}} \quad (24)$$

The summation term in Eq. (23) represents  $\text{CO}^*$ -consumed in the propagation of a chain (rather than in its initiation). At FTS conditions, this term is thus much greater than 1 (since chains are longer than  $\text{C}_{10}$  on average), indicating that most  $\text{CO}^*$  is consumed at sites vicinal to growing chains, rather than on unperturbed  $\text{CO}^*$ -covered surfaces as these chains are unable to migrate on  $\text{CO}^*$ -covered surfaces. As a result, measured FTS activation barriers do not represent enthalpies of isolated  $\text{CO}^*$  activation that initiate each chain (234 kJ mol<sup>-1</sup>, Fig. 3A), but those for  $\text{CO}^*$  activations vicinal to growing chains (average of 136 kJ mol<sup>-1</sup>, Fig. 8A), whose values are similar to reported measured activation barriers (100–150 kJ mol<sup>-1</sup>) on Co [7] and Ru [8] catalysts.

### 3.5. Relative alkylidyne, alkylidene, and alkyl coverages and their kinetic relevance

The results in Section 3.3 confirm that alkylidyne ( $\text{C}_n\text{H}_{2n-1}^*$ ) species (e.g.,  $\text{CH}^*$ ,  $\text{CH}_3\text{C}^*$ ,  $\text{C}_2\text{H}_5\text{C}^*$ ) promote the activation of vicinal  $\text{CO}^*$  species on Ru surfaces by disrupting dense  $\text{CO}^*$  adlayers and thus creating an activation space that avoids the need to desorb  $\text{CO}^*$ . These surface alkylidyne are stable at high  $\text{CO}^*$  coverages and do





**Fig. 8.** (A) Enthalpy and (B) free energy differences (500 K) for forming  $\text{CH}^*\text{O}^*-\text{H}^*$  from  $\text{CO}^*$  vicinal to a  $\text{CO}^*$  ( $\Delta H_{\gamma 1}$  and  $\Delta G_{\gamma 1}$ ) and hydrocarbon chains ( $\text{C}_n\text{H}_{2n-1}^*$ ,  $\Delta H_{\gamma(n+1)}$  and  $\Delta G_{\gamma(n+1)}$ ,  $n = 1-4$ ).  $\text{CO}^*$  desorption energies ( $-\Delta H_{\text{ads},\text{CO}} = 104 \text{ kJ mol}^{-1}$  and  $-\Delta G_{\text{ads},\text{CO}} = 23 \text{ kJ mol}^{-1}$ ) are also shown as it is required for forming  $\text{CH}^*\text{O}^*-\text{H}^*$  from two  $\text{CO}^*$  species on the surface (during initiation). The average  $\Delta H_{\gamma n}$  and  $\Delta G_{\gamma n}$  ( $n = 2-5$ ) values (134 and 213  $\text{kJ mol}^{-1}$ , respectively) are shown by the dashed line. Tables containing energies for the full H-assisted  $\text{CO}^*$  activation pathways vicinal to a  $\text{CO}^*$ ,  $\text{CH}^*$ ,  $\text{CH}_3\text{C}^*$ ,  $\text{C}_2\text{H}_5\text{C}^*$ , and  $\text{C}_3\text{H}_7\text{C}^*$  are shown in the SI (Tables S2–S6).

not decompose which is consistent with previous studies [48] that show  $\text{CO}^*$  block ethylidyne dehydrogenation paths and enhance its ability to react with other hydrocarbon surface intermediates. It seems plausible that other chemisorbed species, such as  $\text{C}^*$ , alkylidenes ( $\text{C}_n\text{H}_{2n}^*$ ), or alkyls ( $\text{C}_n\text{H}_{2n+1}^*$ ) can also create such spaces and thus promote  $\text{CO}^*$  activation in their vicinity.

The ratios of the rates of  $\text{CO}^*$  activation vicinal to an alkylidene ( $r_{\text{CO},\text{C}_n\text{H}_{2n}^*}$ ) or alkyl ( $r_{\text{CO},\text{C}_n\text{H}_{2n+1}^*}$ ) chain to that at a location vicinal to an alkylidyne chain ( $r_{\text{CO},\text{C}_n\text{H}_{2n-1}^*}$ ) are given by:

$$\frac{r_{\text{CO},\text{C}_n\text{H}_{2n}^*}}{r_{\text{CO},\text{C}_n\text{H}_{2n-1}^*}} = \frac{[\text{C}_n\text{H}_{2n}^*]}{[\text{C}_n\text{H}_{2n-1}^*]} \exp\left(\frac{-\Delta G_{\gamma,\text{C}_n\text{H}_{2n}^*} + \Delta G_{\gamma,\text{C}_n\text{H}_{2n-1}^*}}{RT}\right) \quad (25)$$

$$\frac{r_{\text{CO},\text{C}_n\text{H}_{2n+1}^*}}{r_{\text{CO},\text{C}_n\text{H}_{2n-1}^*}} = \frac{[\text{C}_n\text{H}_{2n+1}^*]}{[\text{C}_n\text{H}_{2n-1}^*]} \exp\left(\frac{-\Delta G_{\gamma,\text{C}_n\text{H}_{2n+1}^*} + \Delta G_{\gamma,\text{C}_n\text{H}_{2n-1}^*}}{RT}\right) \quad (26)$$

respectively. These ratios depend in turn on the relative coverages of alkylidene or alkyl chains to those of alkylidynes and on the difference in the respective free energy barriers to form  $\text{CH}^*\text{O}^*-\text{H}^*$  from

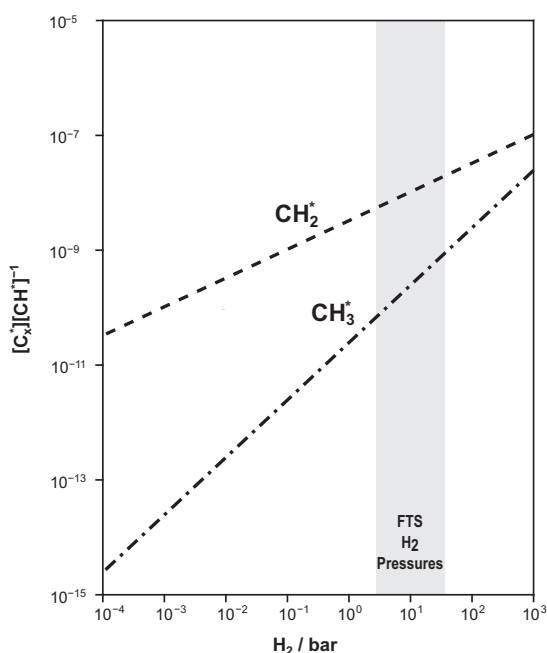
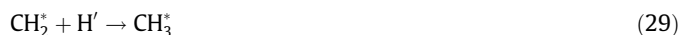
$\text{CO}^*$  and  $\text{H}_2$  ( $\Delta G_{\gamma}^{\text{H}_2}$ ) at these various locations, as given by Eqs. (25) and (26). In assessing the contributions to  $\text{CO}$  activation at these different locations, we first consider the  $[\text{C}_n\text{H}_{2n}^*]/[\text{C}_n\text{H}_{2n-1}^*]$  and  $[\text{C}_n\text{H}_{2n+1}^*]/[\text{C}_n\text{H}_{2n-1}^*]$  coverage ratios for these  $\text{C}_1$  species.  $\text{CH}^*$  binds at three-fold sites (Fig. 4D) and can react with  $\text{H}^*$  (from quasi-equilibrated  $\text{H}_2$  dissociation, Step 2 in Scheme 1) to form  $\text{CH}_2^*$ :



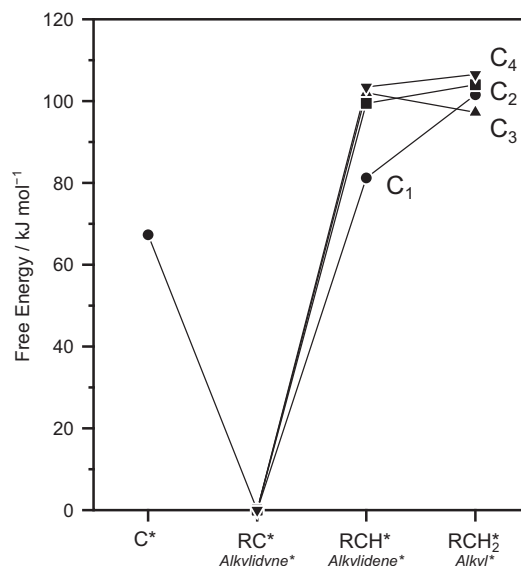
for which, the DFT-derived  $\Delta H_{\text{rxn}}$  value is  $51 \text{ kJ mol}^{-1}$  and the  $\Delta G_{\text{rxn}}$  value is  $81 \text{ kJ mol}^{-1}$  (500 K, 1 bar  $\text{H}_2$ ). The assumption of quasi-equilibrium for Eq. (27) then leads to a maximum  $[\text{CH}_2^*]/[\text{CH}^*]$  ratio that depends on  $\Delta G_{\text{rxn},27}$  and on the  $\text{H}_2$  pressure  $[(\text{H}_2)]$  in bar:

$$\frac{[\text{CH}_2^*]}{[\text{CH}^*]} = e^{\left(\frac{-\Delta G_{\text{rxn},27}}{RT}\right)} (\text{H}_2)^{0.5} \quad (28)$$

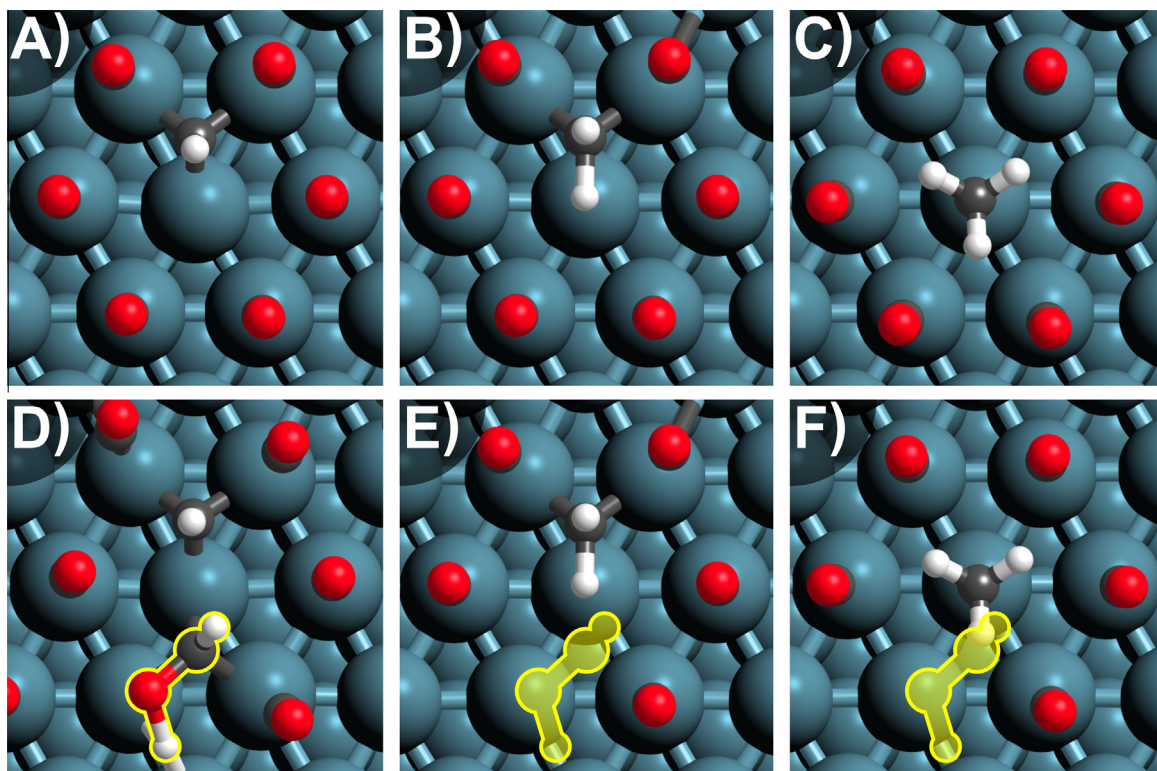
This ratio is  $\sim 10^{-8}$  at 10 bar  $\text{H}_2$  and 500 K (Fig. 9). A similar analysis for the formation of  $\text{CH}_3^*$  via  $\text{CH}_2^*$  reactions with  $\text{H}^*$ :



**Fig. 9.** Ratios of  $\text{CH}_2^*$  and  $\text{CH}_3^*$  to  $\text{CH}^*$  at 500 K as a function of  $\text{H}_2$  pressure (bar).  $\text{H}_2$  pressures typical of FTS are shown in a shaded region.



**Fig. 10.** Free energies ( $\text{kJ mol}^{-1}$ , 500 K, 1 bar  $\text{H}_2$ ) to form alkylidene ( $\text{RCH}^*$ ,  $\text{R} = \text{H}$ ,  $\text{CH}_3$ ,  $\text{C}_2\text{H}_5$ ,  $\text{C}_3\text{H}_7$ ) and alkyl ( $\text{RCH}_2^*$ ) species from C1–C4 alkylidynes ( $\text{RC}^*$ ) (C1: ●, C2: ■, C3: ▲, C4: ▼) and a stoichiometric amount of  $\text{H}_2$ . Also shown is the free energy to form  $\text{C}^*$  (and  $\frac{1}{2}\text{H}_2(\text{g})$ ) from  $\text{CH}^*$ .



**Fig. 11.** (A)–(D) DFT-calculated structures of CH\*, CH<sub>2</sub>\*, CH<sub>3</sub>\*, and the \*CHO–H\* transition state vicinal to a CH\*. (E)–(F) Overlays of DFT-calculated structures for CH<sub>2</sub>\* and CH<sub>3</sub>\* with the \*CHO–H\* transition state from (D).

gives a maximum [CH<sub>3</sub>\*]/[CH\*] ratio when equilibrated:

$$\frac{[\text{CH}_3^*]}{[\text{CH}^*]} = e^{\left(\frac{-\Delta G_{\text{rxn},29} - \Delta G_{\text{rxn},27}}{RT}\right)} (\text{H}_2) \quad (30)$$

This value is  $\sim 10^{-10}$  at 10 bar H<sub>2</sub> and 500 K (Fig. 9). These very low concentrations of CH<sub>2</sub>\* and CH<sub>3</sub>\* relative to CH\* reflect the large  $\Delta G_{\text{rxn}}$  of Eqs. (27) and (29) (81 and 18 kJ mol<sup>−1</sup> at 500 K, 1 bar H<sub>2</sub>).

The small concentrations of CH<sub>2</sub>\* and CH<sub>3</sub>\* relative to CH\* reflect their large  $\Delta H_{\text{rxn}}$  (51 and 46 kJ mol<sup>−1</sup>, respectively) and  $\Delta G_{\text{rxn}}$  (81 and 102 kJ mol<sup>−1</sup>, respectively) (500 K) for their formation from CH\* and the stoichiometric amount of H<sub>2</sub> (Fig. 10). The  $\Delta G_{\text{rxn}}$  values for the corresponding formation of C<sub>2</sub>–C<sub>4</sub> alkylidenes from alkylidynes (and ½H<sub>2</sub>(g)) are 99, 102, and 103 kJ mol<sup>−1</sup>, respectively, and thus even larger than for similar reactions of C<sub>1</sub>\* species (by  $\sim 20$  kJ mol<sup>−1</sup>; Fig. 10); the  $\Delta G_{\text{rxn}}$  values for the formation of C<sub>2</sub>–C<sub>4</sub> alkyls from alkylidynes are 104, 97, and 107 kJ mol<sup>−1</sup>, respectively, and thus similar to those for the respective C<sub>1</sub>\* species (102 kJ mol<sup>−1</sup>, 500 K; Fig. 10). These  $\Delta G_{\text{rxn}}$  values indicate that alkylidynes are also the predominant C<sub>2</sub>–C<sub>4</sub> species present as growing chains on Ru surfaces. At all conditions relevant to FTS practice, they represent the most abundant form of adsorbed chains, with alkyls and alkylidenes present as minor species (Eqs. (25) and (26); Fig. 9). These relative abundances cast doubt upon C–C bond formation through alkylidene insertions into alkyl chains suggested in the literature [19,20,50,51], in favor of growth via alkylidyne species, as suggested elsewhere [22–25].

In light of these relative coverages, the free energy barriers to form CH\*O–H\* ( $\Delta G_{\text{y}}^{\ddagger}$ ) near alkylidene and alkyl chains would have to be  $\sim 100$  kJ mol<sup>−1</sup> lower than the free energy barriers for forming CH\*O–H\* near alkylidyne species for the CO\* activation near alkylidene or alkyl chains to contribute to chain growth. First, we note that the  $\Delta G_{\text{y}}^{\ddagger}$  for CO\* activation near vacancies (207 kJ mol<sup>−1</sup>) was similar to that near C<sub>1</sub>–C<sub>4</sub> alkylidyne chains (average of

213 kJ mol<sup>−1</sup>), indicating that the effects of co-adsorbates on  $\Delta G_{\text{y}}^{\ddagger}$  are generally weakly repulsive. Furthermore, the binding modes of alkylidene and alkyl species (shown in Fig. 11B and 11C for C<sub>1</sub> species) would lead to greater interference between those chains and CH\*O–H\* (shown by a yellow-shaded overlay in Fig. 11E and 11F), in contrast to CH\*O–H\* formation near CH\* (Fig. 11D). Alkylidyne chains are the most abundant form of growing chains on the catalyst surface (Fig. 9) and they effectively disrupt CO\* adlayers to facilitate further activations of CO\* species and thus rapidly increase the rate of chain growth over that of chain initiation.

#### 4. Conclusions

Chains grow much more rapidly than they initiate during FTS on Ru and Co surfaces, which appears inconsistent with chain growth via CH<sub>x</sub>\*-insertion (carbene-like) mechanisms as CH<sub>x</sub>\* species have to be created via CO\* activation processes identical to those which initiate chains. Here, this inconsistency is resolved through the use of DFT calculations at the high CO\* coverages (1.044 ML) relevant to FTS by demonstrating that alkylidyne hydrocarbon chains (C<sub>n</sub>–H<sub>2n–1</sub>\*, *n* = 1–4) disrupt the CO\* adlayer and permit H-assisted CO\* activation without CO\* desorption, leading to activation enthalpies and free energies  $\sim 100$  and  $\sim 15$  kJ mol<sup>−1</sup> lower for CO\* activation near chains than within unperturbed monolayers. Alkylidyne species are much more abundant (by  $\sim 10^8$ ) than alkylidene or alkyl species which do not permit CO\* activation at vicinal sites. Once formed, CH\* species can easily form C–C bonds with hydrocarbon chains (activation free energies  $< 100$  kJ mol<sup>−1</sup>), ultimately leading to observed alkene and alkane products. Co follows the same rate law and displays similar product distributions and measured activation barriers as Ru, indicating that the mechanism for FTS is likely similar on both metals. Thus, we consider the

ability of CO\* to activate more rapidly near chains to be applicable to both metals.

## Acknowledgments

The authors acknowledge the financial support and computational resources provided by BP through the X-Conversion Consortium (BP-XC<sup>2</sup>). We thank Drs. Craig Plaisance, Corneliu Buda, Jay Labinger, John Shabaker, and George Huff for helpful technical discussions. Computational resources were also provided by the Molecular Science Computing Facility (MSCF) in the William R. Wiley Environmental Molecular Sciences Laboratory, a national scientific user facility sponsored by the U.S. Department of Energy, Office of Biological and Environmental Research at the Pacific Northwest National Laboratory.

## Appendix A. Supplementary material

Supplementary data associated with this article can be found, in the online version, at <http://dx.doi.org/10.1016/j.jcat.2016.01.010>.

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